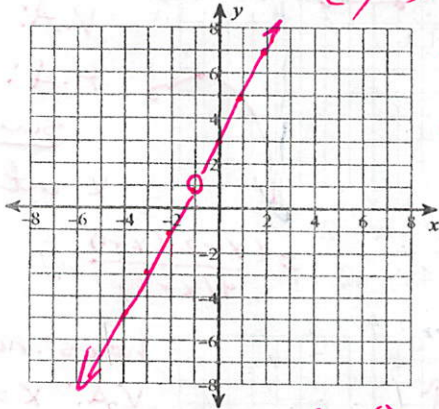


7.4 Homework

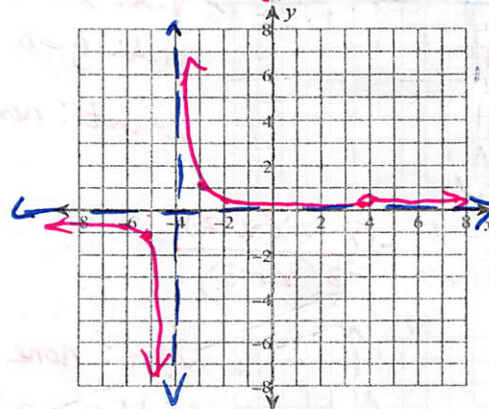
Graph each of the following WITHOUT desmos and state the domain and range. Identify all holes and asymptotes.

1) $y = \frac{2x^2 + 5x + 3}{x + 1}$ $\frac{(2x+3)(x+1)}{(x+1)}$ hole: $x = -1$



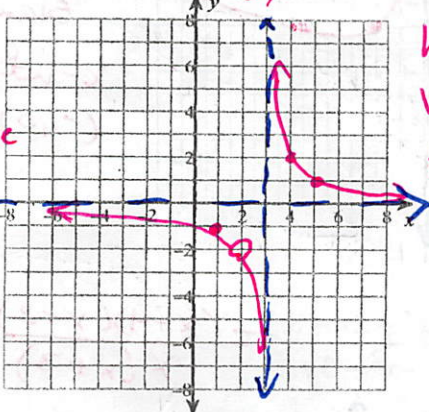
D: $x \neq -1$
R: $y \neq 1$

2) $y = \frac{x - 4}{x^2 - 16} = \frac{(x-4)}{(x-4)(x+4)} = \frac{1}{x+4}$



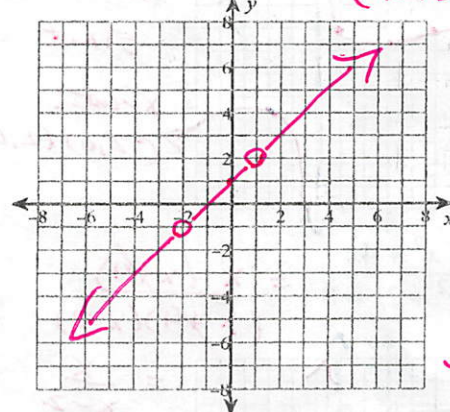
hole: $x = -4$
V.A: $x = -4$
H.A: $y = 0$
D: $x \neq -4$
 $x \neq -4$
R: $y \neq 0$
 $y \neq \frac{1}{8}$

3) $y = \frac{2x - 4}{x^2 - 5x + 6} = \frac{2(x-2)}{(x-2)(x-3)} = \frac{2}{x-3}$



hole: $x = 2$
V.A: $x = 3$
H.A: $y = 0$
D: $x \neq 2$
 $x \neq 3$
R: $y \neq 0$
 $y \neq -2$

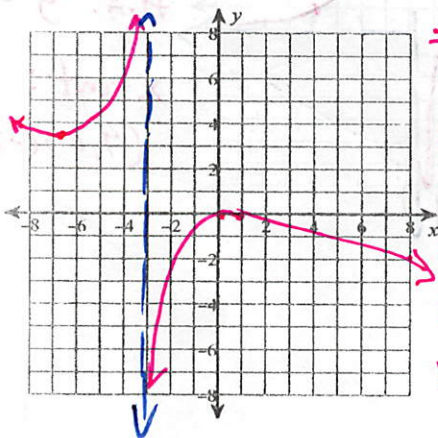
4) $y = \frac{x^3 + 2x^2 - x - 2}{x^2 + x - 2} = \frac{x^2(x+2) - 1(x+2)}{(x+2)(x-1)} = \frac{(x+2)(x^2-1)}{(x+2)(x-1)} = \frac{(x+2)(x-1)(x+1)}{(x+2)(x-1)} = x+1$



holes: $x = -2$
 $x = 1$
D: $x \neq -2$
 $x \neq 1$
R: $y \neq 2$
 $y \neq -1$

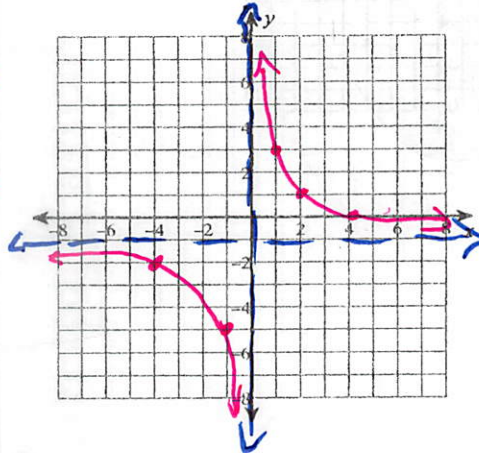
Identify the holes, vertical asymptotes, horizontal asymptotes, and x and y-intercepts of each. Then sketch the graph using Desmos.com.

5) $f(x) = \frac{x^3 - x}{-4x^2 - 16x - 12} = \frac{x(x^2 - 1)}{-4(x^2 + 4x + 3)}$



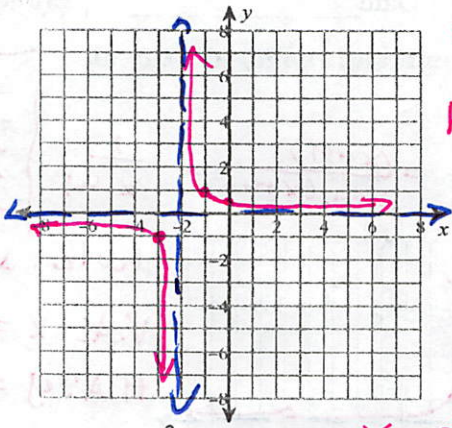
$= \frac{x(x+1)(x-1)}{-4(x+3)(x+1)}$
hole: $x = -1$
V.A: $x = -3$
H.A: none
Slant
x-int: $(0, 0)$ and $(1, 0)$

6) $f(x) = \frac{-x + 4}{x}$



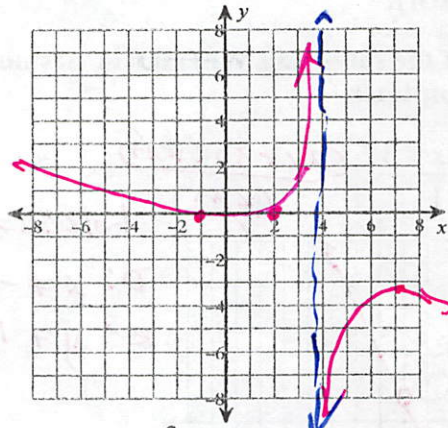
holes: none
V.A: $x = 0$
H.A: $y = -1$
x-int: $(4, 0)$

$$7) f(x) = \frac{x-1}{x^2+x-2} = \frac{x-1}{(x+2)(x-1)} = \frac{1}{x+2}$$



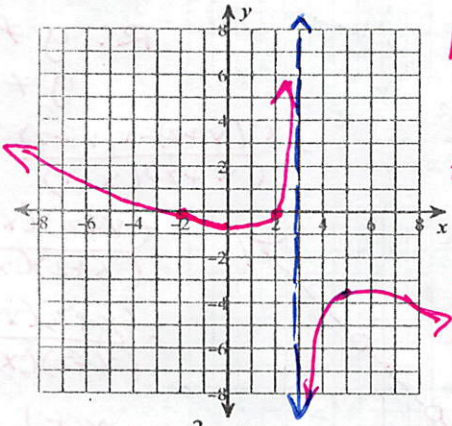
$= \frac{1}{x+2}$
 holes: $x = 1$
 V.A.: $x = -2$
 H.A.: $y = 0$
 x-int: none

$$8) f(x) = \frac{x^3 - x^2 - 2x}{-4x^2 + 16x} = \frac{x(x^2 - x - 2)}{-4x(x-4)} = \frac{x(x-2)(x+1)}{-4(x-4)}$$



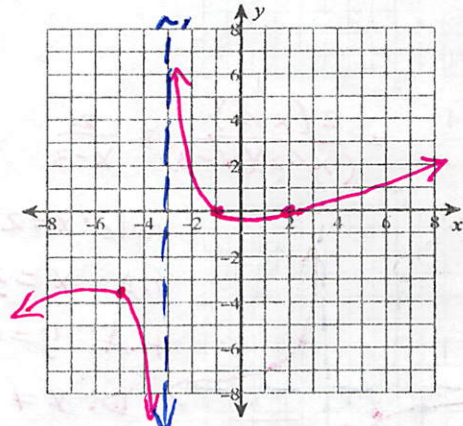
$\frac{(x-2)(x+1)}{-4(x-4)}$
 holes: $x = 0$
 V.A.: $x = 4$
 H.A.: none
 slant
 x-int: $(2,0)$
 $(-1,0)$

$$9) f(x) = \frac{x^2 - 4}{-3x + 9} = \frac{(x+2)(x-2)}{-3(x-3)}$$



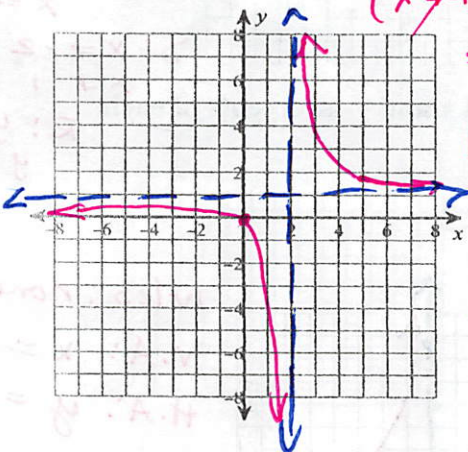
holes: none
 V.A.: $x = 3$
 H.A.: none
 slant
 x-int: $(-2,0)$
 $(2,0)$

$$10) f(x) = \frac{x^2 - x - 2}{4x + 12} = \frac{(x-2)(x+1)}{4(x+3)}$$



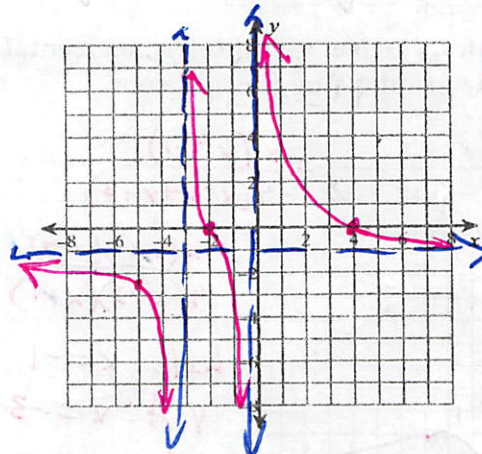
holes: none
 V.A.: $x = -3$
 H.A.: none
 slant
 x-int: $(-1,0)$
 $(2,0)$

$$11) f(x) = \frac{x^2 + 4x}{x^2 + 2x - 8} = \frac{x(x+4)}{(x+4)(x-2)} = \frac{x}{x-2}$$



hole: $x = -4$
 V.A.: $x = 2$
 H.A.: $y = 1$
 x-int: $(0,0)$

$$12) f(x) = \frac{x^2 - 2x - 8}{-x^2 - 3x} = \frac{(x-4)(x+2)}{-x(x+3)}$$



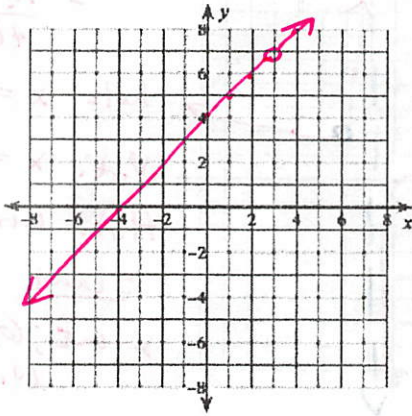
holes: none
 V.A.: $x = 0$
 $x = -3$
 H.A.: $y = -1$
 x-int: $(4,0)$
 $(-2,0)$

Section 7.4 (Notes)

Graphing Rational Functions without a calculator:

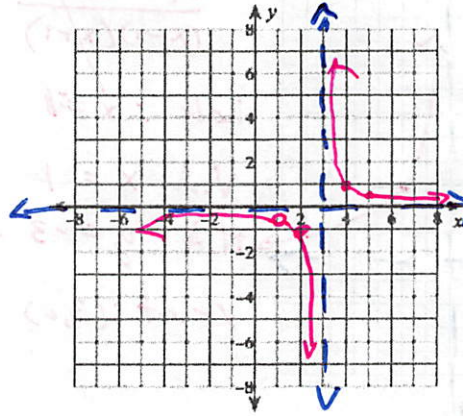
Find the vertical and horizontal asymptotes and sketch a graph of the function:

$$f(x) = \frac{x^2+x-12}{x-3} = \frac{(x+4)(x-3)}{(x-3)}$$



hole: $x=3$
V.A: none
H.A: none

$$f(x) = \frac{x-1}{x^2-4x+3} = \frac{x-1}{(x-3)(x-1)} = \frac{1}{x-3}$$

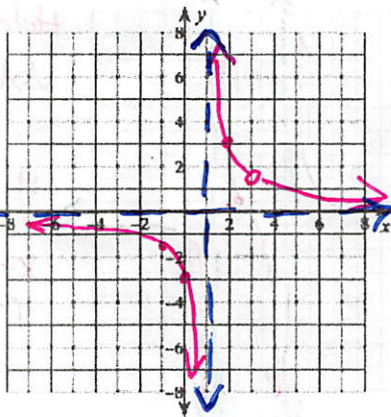


hole: $x=1$
V.A: $x=3$
H.A: $y=0$

x	y
1	1/2
2	-1
4	1
5	1/2

→ hole

$$f(x) = \frac{3x-9}{x^2-4x+3} = \frac{3(x-3)}{(x-3)(x-1)} = \frac{3}{x-1}$$

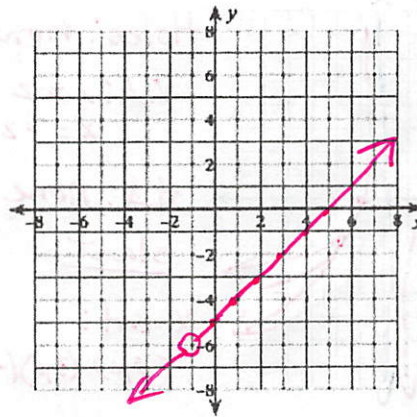


hole: $x=3$
V.A: $x=1$
H.A: $y=0$

x	y
-1	-3/2
0	-3
2	3
3	3/2

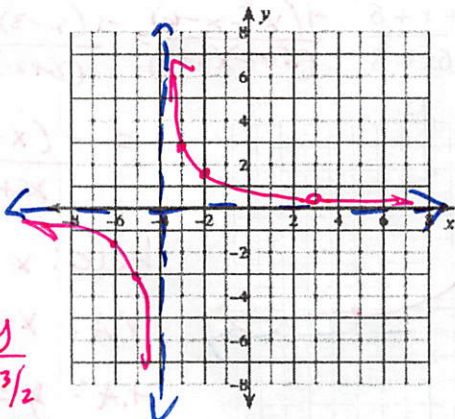
hole

$$f(x) = \frac{x^2-4x-5}{x+1} = \frac{(x-5)(x+1)}{(x+1)}$$



hole: $x=-1$
V.A: none
H.A: none

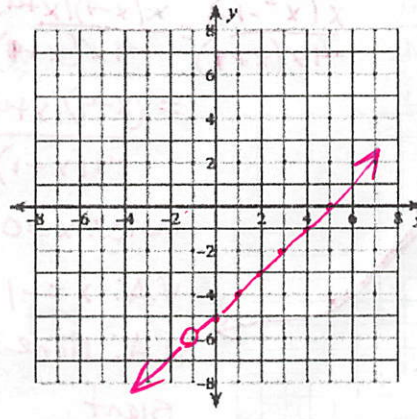
$$f(x) = \frac{3x-9}{x^2+x-12} = \frac{3(x-3)}{(x-3)(x+4)} = \frac{3}{x+4}$$



hole: $x=-3$
V.A: $x=-4$
H.A: $y=0$

x	y
-6	-3/2
-5	-3
-3	3
-2	3/2

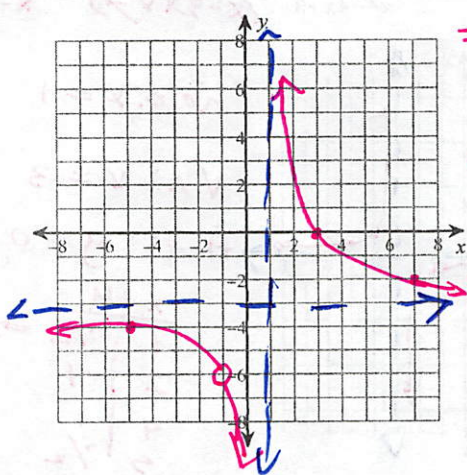
$$f(x) = \frac{x^2-4x-5}{x+1} = \frac{(x-5)(x+1)}{(x+1)}$$



hole: $x=-1$
V.A: none
H.A: none

Identify the points of discontinuity, holes, vertical asymptotes, x-intercepts, and horizontal asymptote of each. Then sketch the graph using Desmos.

$$1) f(x) = \frac{-3x^2 + 6x + 9}{x^2 - 1} = \frac{-3(x^2 - 2x - 3)}{(x-1)(x+1)}$$



$$= \frac{-3(x-3)(x+1)}{(x-1)(x+1)}$$

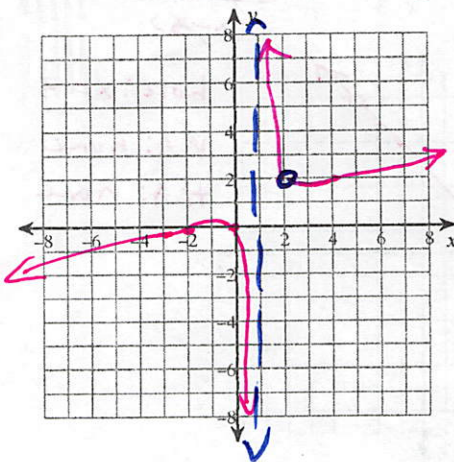
hole: $x = -1$

V.A: $x = 1$

H.A: $y = -3$

X-int: $(3, 0)$

$$2) f(x) = \frac{x^3 - 4x}{4x^2 - 12x + 8}$$



$$\frac{x(x^2 - 4)}{4(x^2 - 3x + 2)} = \frac{x(x/2)(x+2)}{4(x/2)(x-1)}$$

$$= \frac{x(x+2)}{4(x-1)}$$

hole: $x = 2$

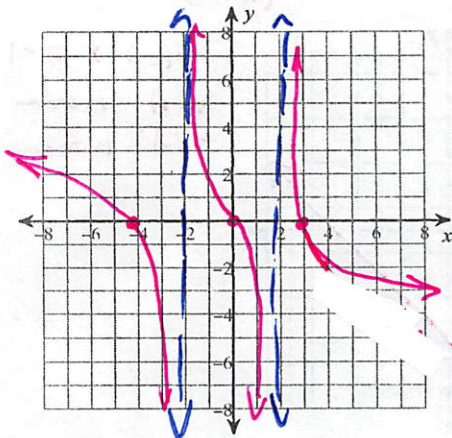
V.A: $x = 1$

H.A: none

Slant

X-int: $(0, 0)$
 $(0, -2)$

$$3) f(x) = \frac{x^3 + x^2 - 12x}{-3x^2 + 12} = \frac{x(x^2 + x - 12)}{-3(x^2 - 4)} = \frac{x(x+4)(x-3)}{-3(x+2)(x-2)}$$



Holes: none

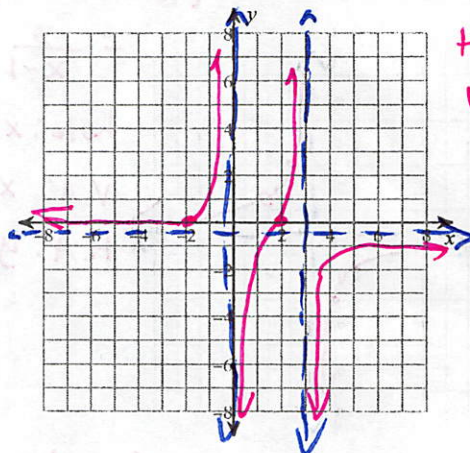
V.A: $x = 2$
 $x = -2$

H.A: none

slant

X-int: $(0, 0)$ $(3, 0)$ $(-4, 0)$

$$4) f(x) = \frac{x^2 - 4}{-3x^2 + 9x} = \frac{(x+2)(x-2)}{-3x(x-3)}$$



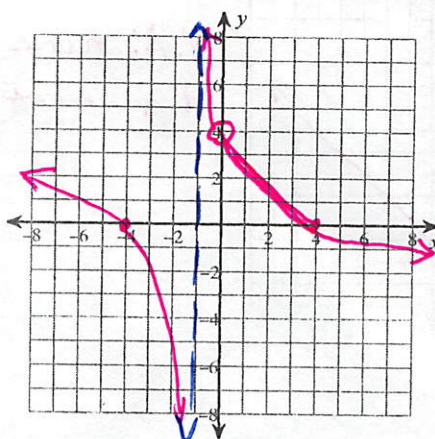
Holes: none

V.A: $x = 0$
 $x = 3$

H.A: $y = -\frac{1}{3}$

X-int: $(-2, 0)$ $(2, 0)$

$$5) f(x) = \frac{x^3 - 16x}{-4x^2 - 4x} = \frac{x(x^2 - 16)}{-4x(x+1)} = \frac{x(x-4)(x+4)}{-4x(x+1)}$$



$$= \frac{(x-4)(x+4)}{-4(x+1)}$$

hole: $x = 0$

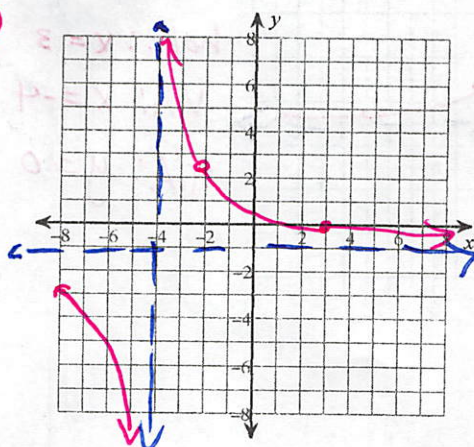
V.A: $x = -1$

H.A: None

Slant

X-int: $(4, 0)$ $(-4, 0)$

$$6) f(x) = \frac{-x^2 + x + 6}{x^2 + 6x + 8} = \frac{-1(x^2 - x - 6)}{(x+2)(x+4)} = \frac{-1(x-3)(x+2)}{(x+2)(x+4)}$$



$$= \frac{-(x-3)}{x+4}$$

hole: $x = -2$

V.A: $x = -4$

H.A: $y = -1$

X-int: $(3, 0)$