

Section 7.2

Find the LCM of each monomial or polynomial expression.

1) $8x^2y, 24xy^3$

$24x^2y^3$

2) $30a^3b, 40ab$

$120a^3b$

3) $2x+4, x+2$

$2(x+2); (x+2)$

$2(x+2)$

4) $x^2-16, x+4$

$(x-4)(x+4); (x+4)$

$(x-4)(x+4)$

5) $x^2-2x-15, x^2+5x+6$

$(x-5)(x+3); (x+2)(x+3)$

$(x-5)(x+3)(x+2)$

6) $x+2, x+3$

$(x+2)(x+3)$

Simplify each expression. (Like Denominators)

7) $\frac{x+6y}{18y} + \frac{x+5y}{18y}$

$\frac{2x+11y}{18y}$

8) $\frac{4x-3y}{10x} - \frac{x+3y}{10x}$

$\frac{3x-6y}{10x}$

9) $\frac{x+5y}{8yx^3} - \frac{x-4y}{8yx^3}$

$= \frac{9y}{8yx^3} = \frac{9}{8x^3}$

10) $\frac{x-1}{x-8} - \frac{x+3}{x-8}$

$\frac{-4}{x-8}$

11) $\frac{4v+2}{4(v-5)} + \frac{v-3}{4(v-5)}$

$\frac{5v-1}{4(v-5)}$

12) $\frac{b+5}{b^2-11b+5} + \frac{b+4}{b^2-11b+5}$

$\frac{2b+9}{b^2-11b+5}$

Simplify each expression. (Unlike Denominators-Monomials)

13) $\frac{4y}{4y^2} - \frac{5x}{5xy} = \frac{1}{y} - \frac{1}{y} \neq 0$

14) $\frac{6}{3} - \frac{6}{5x} = \frac{2}{1} - \frac{6}{5x} = \frac{10x}{5x} - \frac{6}{5x}$

15) $\frac{2m}{3n^3} - \frac{4n}{6mn^2} = \frac{2m}{3n^3} - \frac{2}{3mn}$

$= \frac{2m^2}{3mn^3} - \frac{2n^2}{3mn^3} = \frac{2m^2-2n^2}{3mn^3}$

16) $\frac{2}{6} - \frac{5x}{3xy} = \frac{1}{3} - \frac{5}{3y} = \frac{10x-6}{5x}$

$= \frac{y}{3y} - \frac{5}{3y} = \frac{y-5}{3y}$

17) $\frac{2}{5v^2} + \frac{3}{6u^2}$

$\frac{12u^2}{30v^2u^2} + \frac{15v^2}{30v^2u^2} = \frac{12u^2+15v^2}{30v^2u^2}$

$= \frac{3(4u^2+5v^2)}{30v^2u^2} = \frac{4u^2+5v^2}{10v^2u^2}$

18) $\frac{5}{2u^2v} - \frac{3v}{5u^2v}$

$= \frac{25}{10u^2v} - \frac{6v}{10u^2v} = \frac{25-6v}{10u^2v}$

Simplify each expression. (Unlike Denominators-Polynomials)

$$\begin{aligned}
 19) \quad & \frac{6}{x-4} - \frac{3x}{x+3} \\
 &= \frac{6(x+3)}{(x-4)(x+3)} + \frac{-3x(x-4)}{(x-4)(x+3)} \\
 &= \frac{6x+18-3x^2+12x}{(x-4)(x+3)} \\
 &= \boxed{\frac{-3x^2+18x+18}{(x-4)(x+3)}}
 \end{aligned}$$

$$\begin{aligned}
 21) \quad & \frac{5}{n-4} - \frac{3n}{n^2-7n+12} \\
 &= \frac{5}{n-4} - \frac{3n}{(n-4)(n-3)} \\
 &= \frac{5(n-3)}{(n-4)(n-3)} + \frac{-3n}{(n-4)(n-3)} \\
 &= \frac{5n-15-3n}{(n-4)(n-3)} = \boxed{\frac{2n-15}{(n-4)(n-3)}}
 \end{aligned}$$

$$\begin{aligned}
 23) \quad & \frac{6}{y^2-2y-35} + \frac{4}{y^2+9y+20} \\
 &= \frac{6}{(y-7)(y+5)} + \frac{4}{(y+5)(y+4)} \\
 &= \frac{6(y+4)}{(y-7)(y+5)(y+4)} + \frac{4(y-7)}{(y-7)(y+5)(y+4)} \\
 &= \frac{6y+24+4y-28}{(y-7)(y+5)(y+4)} \\
 &= \boxed{\frac{10y-4}{(y-7)(y+5)(y+4)}}
 \end{aligned}$$

$$\begin{aligned}
 20) \quad & \frac{4n}{3} - \frac{n+3}{6n+6} = \frac{4n}{3} - \frac{n+3}{2 \cdot 3(n+1)} \\
 &= \frac{4n \cdot 2(n+1)}{6(n+1)} + \frac{-(n+3)}{6n+6} \\
 &= \frac{8n^2+8n-n-3}{6n+6} \\
 &= \boxed{\frac{8n^2+7n-3}{6n+6}}
 \end{aligned}$$

$$\begin{aligned}
 22) \quad & \frac{3}{n-3} + \frac{2n}{n^2-9} = \frac{3}{n-3} + \frac{2n}{(n-3)(n+3)} \\
 &= \frac{3(n+3)}{(n-3)(n+3)} + \frac{2n}{(n-3)(n+3)} \\
 &= \frac{3n+9+2n}{(n-3)(n+3)} \\
 &= \boxed{\frac{5n+9}{(n-3)(n+3)}}
 \end{aligned}$$

$$\begin{aligned}
 24) \quad & \frac{5}{a-4} + \frac{6}{a-3} \\
 &= \frac{5(a-3)}{(a-4)(a-3)} + \frac{6(a-4)}{(a-4)(a-3)} \\
 &= \frac{5a-15+6a-24}{(a-4)(a-3)} \\
 &= \boxed{\frac{11a-39}{(a-4)(a-3)}}
 \end{aligned}$$

Simplify each expression. (Complex Fractions)

$$25) \frac{\frac{\frac{m}{5} + \frac{m}{2}}{2}}{m^2} = \frac{\frac{2m}{10} + \frac{5m}{10}}{\frac{2}{m^2}}$$

$$= \frac{\frac{7m}{10}}{\frac{2}{m^2}} = \frac{7m}{10} \cdot \frac{m^2}{2}$$

$$= \boxed{\frac{7m^3}{20}}$$

$$26) \frac{\frac{1}{3x} + \frac{36}{x^2}}{\frac{36}{x^2}} \cdot \frac{3x^2}{3x^2}$$

$$= \boxed{\frac{x + 108}{108}}$$

$$27) \frac{\frac{36}{x}}{\frac{x+3}{x} + \frac{x+3}{x^2}} \cdot \frac{x^2}{x^2}$$

$$= \frac{36x}{x(x+3) + (x+3)}$$

$$= \frac{36x}{x^2 + 3x + x + 3}$$

$$= \boxed{\frac{36x}{x^2 + 4x + 3}}$$

$$28) \frac{\frac{a-3}{4a} - \frac{a-3}{4}}{\frac{a-3}{4a}} = \frac{\frac{a-3}{4a} + \frac{-a(a-3)}{4a}}{\frac{a-3}{4a}}$$

$$= \frac{a-3 - a^2 + 3a}{4a} = \frac{-a^2 + 4a - 3}{4a}$$

$$= \frac{(a-3)(a-1)}{4a} \cdot \frac{4a}{a-3} = \frac{-(a-1)}{(a-3)}$$

$$29) \frac{\frac{3u-15}{3}}{\frac{u-5}{3} + \frac{u-5}{u+4}} = \frac{\frac{3(u-5)}{3}}{\frac{(u-5)(u+4) + 3(u-5)}{3(u+4)}}$$

$$= \frac{\frac{3(u-5)}{3}}{\frac{(u-5)(u+4) + 3(u-5)}{3(u+4)}}$$

$$= \frac{3(u-5)}{3} \cdot \frac{3(u+4)}{(u-5)(u+7)} = \boxed{\frac{3(u+4)}{(u+7)^3}}$$

$$30) \frac{\frac{a^2-4a}{3}}{\frac{3}{a} + \frac{3}{a}} = \frac{\frac{a^2-4a}{3}}{\frac{6}{a}} = \frac{a^2-4a}{3} \cdot \frac{a}{6}$$

$$= \boxed{\frac{a^3-4a^2}{18}}$$