

11.1A Trig Functions in Right Triangles

I can evaluate the six trig functions given a right triangle.

Given one trig ratio, I can use the Pythagorean theorem to find the five remaining trig ratios.

I can use trig functions to find missing sides of a right triangle.

I can use inverse trig functions to find missing angles of a right triangle.

Trigonometry is the Greek term meaning _____.

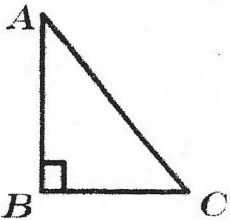
When working with angles we tend to use a variable other than "x". Instead we use _____.

Recognizing the parts

Hypotenuse -

Opposite side -

Adjacent side -



$$\sin \theta =$$

$$\csc \theta =$$

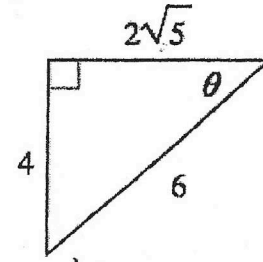
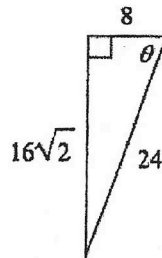
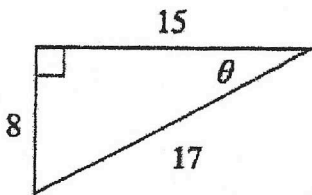
$$\cos \theta =$$

$$\sec \theta =$$

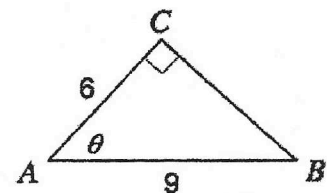
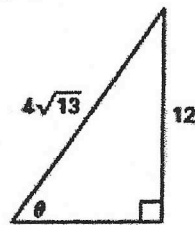
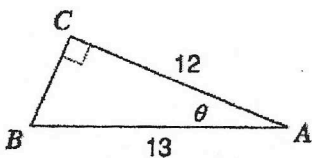
$$\tan \theta =$$

$$\cot \theta =$$

I can evaluate the six trig functions given a right triangle.



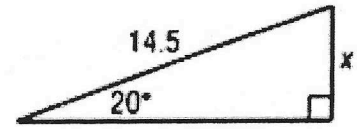
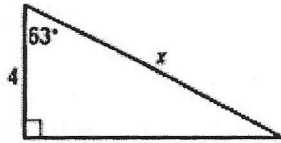
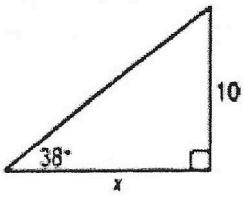
Given one trig ratio, I can use the Pythagorean theorem to find the five remaining trig ratios.



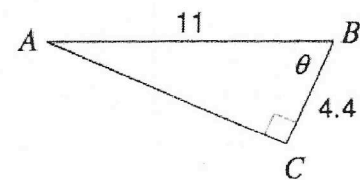
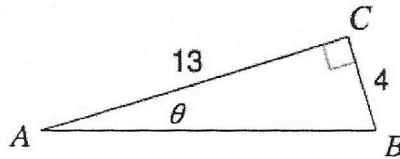
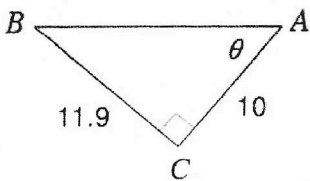
I can use trig functions to find missing sides of a right triangle. (Use $\sin \theta$, $\cos \theta$, $\tan \theta$)

Steps for solving for a missing side of a triangle using trigonometry:

- 1-
- 2-
- 3-
- 4-
- 5-



I can use inverse trig functions to find missing angles of a right triangle. (Use $\sin^{-1} \theta$, $\cos^{-1} \theta$, $\tan^{-1} \theta$)



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I can use trig functions to find missing sides of a right triangle.

I can use inverse trig functions to find missing angles of a right triangle.

Trigonometry is the Greek term meaning many angles.

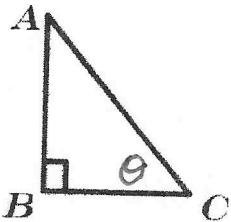
When working with angles we tend to use a variable other than "x". Instead we use θ "theta"

Recognizing the parts

Hypotenuse - opposite right angle (always) - longest side.

Opposite side - opposite the chosen angle.

Adjacent side - adjacent to the chosen angle (not hypotenuse)



Soh Cah Toa

$$\sin \theta = \frac{AB}{AC}$$

$$\csc \theta = \frac{AC}{AB}$$

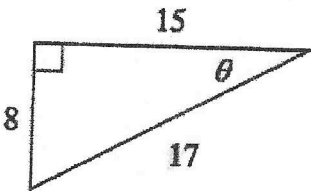
$$\cos \theta = \frac{BC}{AC}$$

$$\sec \theta = \frac{AC}{BC}$$

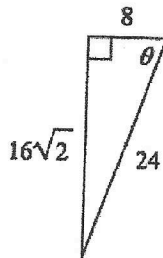
$$\tan \theta = \frac{AB}{BC}$$

$$\cot \theta = \frac{BC}{AB}$$

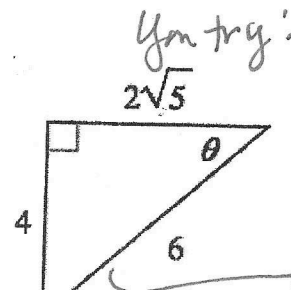
I can evaluate the six trig functions given a right triangle.



$$\begin{aligned} \sin \theta &= \frac{8}{17} & \csc \theta &= \frac{17}{8} \\ \cos \theta &= \frac{15}{17} & \sec \theta &= \frac{17}{15} \\ \tan \theta &= \frac{8}{15} & \cot \theta &= \frac{15}{8} \end{aligned}$$



$$\begin{aligned} \sin \theta &= \frac{16\sqrt{2}}{24} = \frac{2\sqrt{2}}{3} \\ \cos \theta &= \frac{8}{24} = \frac{1}{3} \\ \tan \theta &= \frac{16\sqrt{2}}{8} = 2\sqrt{2} \end{aligned}$$



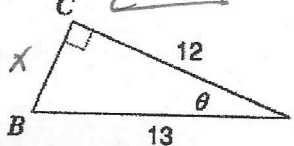
You try!

$$\begin{aligned} \csc \theta &= \frac{6}{4} = \frac{3}{2} \\ \sec \theta &= 3 \\ \tan \theta &= \frac{1}{2} = \frac{\sqrt{2}}{4} \end{aligned}$$

Given one trig ratio, I can use the Pythagorean theorem to find the five remaining trig ratios.

$\cos \theta = \frac{12}{13}$

$a^2 + b^2 = c^2$



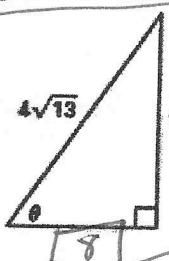
$\sin \theta = \frac{5}{13}$

$\tan \theta = \frac{5}{12}$

$\csc \theta = \frac{13}{5}$

$\sec \theta = \frac{13}{12}$

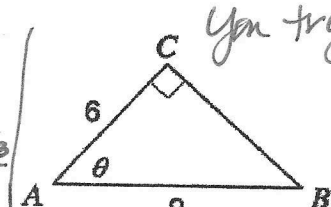
$\cot \theta = \frac{12}{5}$



Given: $\sin \theta = \frac{12}{4\sqrt{3}}$
 $= \frac{3}{\sqrt{3}} = \frac{3\sqrt{3}}{3}$

$x^2 + 12^2 = (4\sqrt{3})^2$
 $x^2 = 8$

$\cos \theta = \frac{8}{4\sqrt{3}} = \frac{2}{\sqrt{3}} = \frac{2\sqrt{3}}{3}$



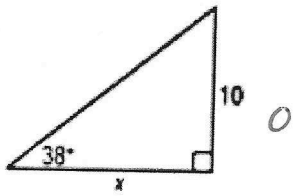
$\csc \theta = \frac{9}{6} = \frac{3}{2}$; $\sec \theta = \frac{9}{3} = 3$

$\tan \theta = \frac{3}{6} = \frac{1}{2}$; $\cot \theta = \frac{2}{1} = 2$

I can use trig functions to find missing sides of a right triangle. (Use $\sin \theta$, $\cos \theta$, $\tan \theta$)

Steps for solving for a missing side of a triangle using trigonometry:

- 1- Identify the given angle.
- 2- Label the sides, (hypotenuse, adjacent, opposite)
- 3- Determine the trig function (sin, cos, or tan)
- 4- Write an equation
- 5- Solve 😊

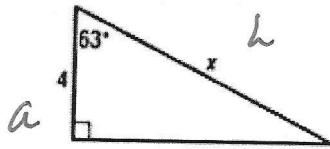


a

$$\frac{\tan 38^\circ}{1} = \frac{10}{x}$$

$$x \cdot \tan 38 = 10$$

$$x = \frac{10}{\tan 38} \approx 12.8$$



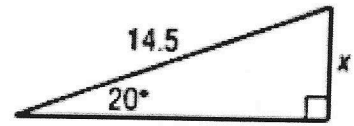
$$\frac{\cos 63}{1} = \frac{4}{x}$$

$$x \cdot \cos 63 = 4$$

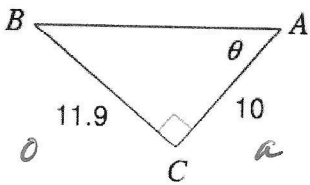
$$x = \frac{4}{\cos 63}$$

$$x \approx 8.8$$

You try 😊



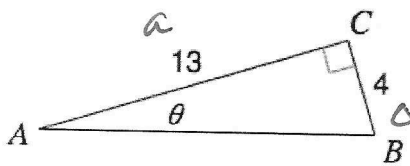
I can use inverse trig functions to find missing angles of a right triangle. (Use $\sin^{-1} \theta$, $\cos^{-1} \theta$, $\tan^{-1} \theta$)



$$\tan \theta = \frac{11.9}{10}$$

$$\theta = \tan^{-1} \left(\frac{11.9}{10} \right)$$

$$\theta \approx 50^\circ$$



$$\tan \theta = \frac{4}{13}$$

$$\theta = \tan^{-1} \left(\frac{4}{13} \right)$$

$$\theta = 17^\circ$$

You try!

