

Section 6.2

I can identify appropriate methods to solve logarithmic equations.

**Methods:**

By converting to exponential form

By condensing an expression

By taking a log of both sides

By changing the bases

**Properties of Logarithms:**

$$a^x = a^y \text{ if only if } x = \underline{\hspace{2cm}}$$

$$\log_b x = \log_b y \text{ if and only if } \underline{\hspace{2cm}}$$

Example:

$$\text{If } \log_3 x = \log_3 8 \text{ then } x = \underline{\hspace{2cm}}$$

$$\log_7(6x - 16) = \log_7(x - 1)$$

$$\log_9(x^2 - 4x) = \log_9(3x - 10)$$

You try ☺

$$\log_3(x - 5) = \log_3(3x - 25)$$

$$\log_7(x^2 - 4) = \log_7(-x + 2)$$

Since  $a^0 = 1$  &

$$a^1 = a$$

$$\log_b x = y \text{ and } b^y = x$$

\_\_\_\_\_ Or \_\_\_\_\_

Solve:

$$\log_8(x - 5) = \frac{2}{3}$$

$$\log_4(5x + 1) = 2$$

You try ☺

$$\log_{16}(x + 12) = \frac{3}{2}$$

$$\log_2(x + 3) = 4$$

Property of Inequality for Logarithmic Functions:

Algebra: if  $b > 1, x > 0$ , and  $\log_b x > y$ , then \_\_\_\_\_

Example:  $\log_2 2x > 2$   $\log_2(8x + 5) > \log_2(6x + 19)$

You try ☺

$$\log_4 8x > 3$$

$$\log_3(8x + 3) > \log_3(5x + 12)$$

Algebra: if  $b > 1, x > 0$ , and  $\log_b x < y$ , then \_\_\_\_\_

Example:  $\log_2(3x + 1) < 4$   $\log_3(3x - 4) < \log_3(x + 1)$

You try ☺

$$\log_3(x + 3) < 3$$

$$\log_2(3x - 4) < \log_2(2x + 7)$$